

Name:

Date:

WORKSHEET :**Absolute Value**

1. $|(-7)| =$

$|(-4)| =$

$|57| =$

2. $|6 \times (-4)| =$

$|(-3) \times (-2)| =$

$|(-2) \times 10| =$

3. $|(-8) + 5| =$

$|(-8) - (-2)| =$

$|(-9)| - 10 =$

4. $|8| \times (-2) =$

$|(-2)| \times |6| =$

$|1 \div (-7)| =$

5. $|(-1) \div (-2)| =$

$|7 \times 4| =$

$8 \times |(-3)| =$

6. $|x| = 2$
 $x =$

$|y| = 5$
 $y =$

$|x| = 10$
 $x =$

7. $\sqrt{2^2} =$

$\sqrt{5^2} =$

$\sqrt{10^2} =$

8. $|x + 1| = 5$
 $x =$

$|x - 1| = 5$
 $x =$

$|x + 2| = 0$
 $x =$

9. $|2x| = 5$
 $x =$

$-2|x + 8| = 2$
 $x =$

$|2x - 1| = 5$
 $x =$

10. $|3y + 5| = y$
 $y =$

$|y - 5| = 2y$
 $y =$

$|-y + 5| = 2y$
 $y =$

ANSWERS :



Absolute Value

1. $|(-7)| = 7$

$|-4| = 4$

$|57| = 57$

2. $|6 \times (-4)| = 24$

$|(-3) \times (-2)| = 6$

$|(-2) \times 10| = 20$

3. $|(-8) + 5| = 3$

$|(-8) - (-2)| = 6$

$|(-9)| - 10 = -1$

4. $|8| \times (-2) = -16$

$|(-2)| \times |6| = 12$

$|1 \div (-7)| = 1/7$

5. $-|(-1) \div (-2)| = -1/2$

$|7 \times 4| = 28$

$8 \times |(-3)| = 24$

6. $|x| = 2$
 $x = \pm 2$

$|y| = 5$
 $y = \pm 5$

$|x| = 10$
 $x = \pm 10$

7. $\sqrt{2^2} = \pm 2$

$\sqrt{5^2} = \pm 5$

$\sqrt{10^2} = \pm 10$

8. $|x + 1| = 5$
Positive Case:
 $x + 1 = 5$
 $x = 4$
Negative Case:
 $-(x + 1) = 5$
 $-x - 1 = 5$
 $-x = 6$
 $x = -6$

$|x - 1| = 5$
Positive Case:
 $x - 1 = 5$
 $x = 6$
Negative Case:
 $-(x - 1) = 5$
 $-x + 1 = 5$
 $-x = 4$
 $x = -4$

$|x + 2| = 0$
Positive Case:
 $x + 2 = 0$
 $x = -2$
Negative Case:
 $-(x + 2) = 0$
 $-x - 2 = 0$
 $-x = 2$
 $x = -2$

If it helps to understand:

" x is an absolute distance
in either direction on the
number line from a
number"

" x is 5 away from -1"

" x is 5 away from +1"

" x is 0 away from -2"

9.	$ 2x = 5$ Positive Case: $2x = 5$ $x = \frac{5}{2}$ Negative Case: $-(2x) = 5$ $-2x = 5$ $-x = \frac{5}{2}$ $x = -\frac{5}{2}$	$-2 x + 8 = 2$ Positive Case: $-2(x + 8) = 2$ $-2x = 18$ $x = -9$ Negative Case: $-2 \cdot -(x + 8) = 2$ $2x + 16 = 2$ $x = -7$ NO SOLUTION	$ 2x - 1 = 5$ Positive Case: $2x - 1 = 5$ $2x = 6$ $x = \frac{6}{2} = 3$ Negative Case: $-(2x - 1) = 5$ $-2x + 1 = 5$ $-2x = 4$ $x = \frac{4}{-2} = -2$
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* There is no solution in this case because the absolute value cannot be a negative result. Plug the results back into the equation.

$$\begin{aligned}-2|-9 + 8| &= -2|-1| = -2(1) \\ \neq 2 \\ -2|-7 + 8| &= -2|1| = -2(1) \neq 2\end{aligned}$$

If it helps to understand:

"x is an absolute distance in either direction on the number line from a number"

Notice it gets increasingly complex to dissect the absolute value equation into a word phrase. This is less essential than being able to solve for the positive and negative case.

"The distance to x is $\frac{5}{2}$ away from 0"

"The distance to x is $\frac{5}{2}$ away from $\frac{1}{2}$ "

10.	$ 3y + 5 = y$ Positive Case: $3y + 5 = y$ $2y + 5 = 0$ $2y = -5$ $y = -\frac{5}{2}$ Negative Case: $-(3y + 5) = y$ $-3y - 5 = y$ $-4y - 5 = 0$ $-4y = 5$ $y = -\frac{5}{4}$	$ y - 5 = 2y$ Positive Case: $y - 5 = 2y$ $-y - 5 = 0$ $-y = 5$ $y = -5$ Negative Case: $-(y - 5) = 2y$ $-y + 5 = 2y$ $-3y + 5 = 0$ $-3y = -5$ $y = -5/-3 = \frac{5}{3}$	$ -y + 5 = 2y$ Positive Case: $-y + 5 = 2y$ $-3y + 5 = 0$ $-3y = -5$ $y = -5/-3 = \frac{5}{3}$ Negative Case: $-(y + 5) = 5$ $y - 5 = 2y$ $-y - 5 = 0$ $-y = 5$ $y = 5/-1 = -5$
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KEY CONCEPTS:

Absolute Value -

a. $|x| \geq 0$

b. $|x \times y| = |x| \times |y|$

c. $|x| = \sqrt{x^2}$ see line 7.

i) The results of the square root of a value squared will be the same as an absolute value symbol. There will be a positive and negative result.

d. Positive and negative solution case e.g. $|2| = \pm 2$ because $|2| = 2$ and $|-2| = 2$

e. Plug results back into equation to check answers

i) No solution (and one or many) is a possible case that must be checked in every equation or inequality. see example in 9.